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# The Structure of Dimolybdenum Carbide by Neutron Diffraction Technique\*

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It is generally believed that Mo<sub>2</sub>C has either the hexagonal C6 cadmium iodide anti-type structure or the related hexagonal L'3 structure. A neutron diffraction study showed that this is not the case. Mo<sub>2</sub>C is only pseudohexagonal and crystallizes with an orthorhombic unit cell with  $a = 4.72_4$ ,  $b = 6.00_4$ , and  $c = 5.19_9$  Å. The atomic arrangement of Mo<sub>2</sub>C presents a new structure type. Space group is  $D_{2h}^{14}$ -Pbcn. Eight molybdenum atoms are in 8(d) with x = 1/4, y = 1/8, z = 1/12 and four carbon atoms are in 4(c) with y = 3/8. The carbon atoms in Mo<sub>2</sub>C arrange themselves in such a way that each molybdenum atom has three nearly planar carbon neighbours.

#### Introduction

In the system molybdenum-carbon two carbide phases exist: The monocarbide, MoC, and the sesquicarbide, Mo<sub>2</sub>C. The structure of the monocarbide was solved earlier by one of the authors (Nowotny, Parthé, Kieffer & Benesovsky, 1954). Recent investigations show, however, that it occurs only with a carbon defect and the formula Mo<sub>3</sub>C<sub>2</sub> has been suggested for this compound (Rudy, Rudy and Benesovsky, 1962). A structure proposal for Mo<sub>2</sub>C dates back as far as 1926. Using the X-ray diffraction technique, Mo<sub>2</sub>C was investigated at that time by Westgren & Phragmen. Due to the small scattering factor of carbon, they could determine with certainty only the spatial arrangement of the metal atoms. They found them to be arranged in a hexagonal close packing. For each two molybdenum atoms, one carbon atom can be tentatively placed in one of the octahedral holes. One thus receives a structure proposal for Mo<sub>2</sub>C as follows:

C6 structure type

Unit cell: Hexagonal: a=3.002 Å, c=4.724 Å Space group:  $D_{3d}^3 - P\overline{3}m1$ Point position: 2 Mo in 2(d): 1/3, 2/3, z; 2/3, 1/3,  $\overline{z}$ with z=1/4

$$1 \text{ C in } 1(a): 0, 0, 0$$

This structure is identical to the first  $CdJ_2(C6)$  structure type, except the metal and non-metal atoms have been interchanged. This type may be called, therefore,  $CdJ_2$ -antitype. However, modern crystal structure compilations (Pearson, 1958) list the Mo<sub>2</sub>C structure as belonging to the L'3 structure type with the one carbon atom statistically distributed between two possible places.

#### L'3 structure type

Same hexagonal unit cell dimensions as above.

- Space group:  $D_{6h}^4 P6_3/mmc$
- Point positions: 2 Mo in 2(c): 1/3, 2/3, 1/4; 2/3, 1/3, 3/4 1 C in 2(a): 0, 0, 0; 0, 0, 1/2

To reveal the true carbon atom positions in  $Mo_2C$ , a neutron diffraction study was undertaken.

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Fig. 1. Mo<sub>2</sub>C powder patterns.

### **Experimental procedure**

The neutron diffraction powder pattern of  $Mo_2C$  was obtained in a manner described in an earlier paper (Parthé & Sadagopan, 1962). The Mo<sub>2</sub>C powder was a gift from the Metallwerk Plansee G.m.b.H. in Reutte, Austria, which also provided the analysis. The Mo<sub>2</sub>C contained 33·3 a./o. bound carbon. There was also 0.8 a./o. free carbon present.

#### Analysis of the diffraction experiments

The neutron diffraction pattern of Mo<sub>2</sub>C is compared with the X-ray diffraction pattern in Fig. 1. To account for the extra neutron diffraction lines, a super cell had to be sought which was based on the hexagonal unit cell determined earlier by X-ray methods. Describing the original hexagonal cell with an orthohexagonal set of axes and doubling of one axes gives the desired result. If  $a_{\rm H}$  and  $c_{\rm H}$  are the hexagonal unit cell dimensions, then the dimensions of the new orthorhombic unit cell are given by:  $a_0 = c_{\rm H}$ ,  $b_0 = 2 a_{\rm H}$ and  $c_0 = a_{\rm H}$ . [/3. This particular setting of axes is chosen to conform with the standard setting of the orthorhombic space group of Mo<sub>2</sub>C which is given below. The new orthorhombic lattice parameters of  $Mo_2C$ , which account for every observed neutron diffraction line, are

$$a = 4.72_4$$
,  $b = 6.00_4$  and  $c = 5.19_9$  Å.

As the positions of the molybdenum atoms are known to be those of a hexagonal close-packed structure, only a limited number of possibilities exist for the positioning of the four carbon atoms. Excellent agreement between calculated and observed intensities was obtained by assuming:

Space group:  $D_{2h}^{14} - Pbcn$ Point positions: 8 Mo in 8(d) with x=1/4, y=1/8, z=1/12. 4 C in 4(c) with y=3/8.

Due to the very special values of the free parameters, many lines which are allowed by the space group were calculated to have zero intensity as can be seen in Table 1. Only the symmetry elements of space group *Pbcn* are present in the structure.

For the calculation of the integrated intensities, a temperature coefficient of  $B=0.5\times10^{-16}$  cm. has been used. The absorption coefficient  $A_{hkl}$  hardly Table 1. Neutron intensity calculation for  $Mo_2C$  with new structure type

 $(\lambda = 1.20 \text{ Å})$  and comparison between the  $|\circ F|$  values for neutrons and X-ray diffraction

New ortho- rhombic indices	Old hexagonal indices	7 ( 8 )	1000 -: ? 0	1000 -: 8 A	r	r	Neutrons	X -rays
hkl	nkil	<i>a</i> (A)	$1000.\sin^2\theta_c$	$1000.\sin^2\theta_0$	1 <sub>c</sub>	10	I'lc	r  c
110		3.710	26.12	26.0	14.8	11.3	10.0	0.9
111		3.021	39.44	39.4	$\begin{bmatrix} 19.6 \\ 0 \end{bmatrix}$ 19.6	18.5	10.0	0.9
020			39.95 J 53.96					(11.0)
	$10\overline{1}0$	(2.601)	53.26				$\begin{pmatrix} 0 \\ 0 \end{pmatrix}$	$\begin{pmatrix} 11.9\\ 11.9 \end{pmatrix}$
200	0002	2.363	64.52	64.4	6.0	7.0	14.1	24.9
102 \	1011	9.978	69·39 \	69.3	<sup>33·3</sup>	100.0	(24.5)	$(22 \cdot 0)$
121 )	1011	2 210	69.39 ∫	55 5	66.6 ∫ 100 0	100 0	(24.5)	$(22 \cdot 0)$
112		2.130	79.38	79.3	7.4	8.3	10.0	0.7
211			03.21		0		0	0
220			104.47		Ŏ		ŏ	õ
130		1.843	106.01	105.5	3.6	3.1	10.0	0.7
122			109.34		0		0	0
202	1012	1.749	117.78		25.8		(28.3)	$(12 \cdot 4)$
221 )	1014	1 720	117.78	118-1	51.6 83.8	83.0	\28.3/	$(12\cdot4)$
131		1.736	119.32		0·4 J		10.0	0.7
113		1.571	145.96	146.4	5.2	5.0	10.0	0.6
310		1.523	155.16		2.5	00	10.0	0.6
222			157.73		0		0	0
132		1.503	159-27	159.0	4.8 72.1	74.9	10.0	0.6
040	$11\overline{2}0$	1.501	159.79		21.6		(42.3)	$\begin{pmatrix} 21 \cdot 9 \\ 21 \cdot 9 \end{pmatrix}$
023 )			159.79 )		43.2)		(42.3/	(21.9/
311		1.462	168.47	168.0	4.6	5.0	10.0	0.6
041			173.10		ô		0	Õ
123		—	175.92		0		0	0
141			189.23		0		0	0
213		_	194.35		0			
304 (	$10\overline{1}3$	1.347	198.43	198.7	$\begin{array}{c} 11.5 \\ 23.0 \end{array}$ 34.5	33.8	$\begin{pmatrix} 24 \cdot 5 \\ 24 \cdot 5 \end{pmatrix}$	$\begin{pmatrix} 17.3\\ 17.2 \end{pmatrix}$
232		_	207.66		200)		0	0
312		1.315	208.42	208.9	3.7	3.7	10.0	0.5
004 )	2020	(1.300)	213.05		0 ) 0		(0)	(9.2)
042 J	2020	(1000)	213.05		0 ) 0		(0)	(9.2)
240	$11\overline{2}2$	1.267	224.31		3·4 6.7		$\begin{pmatrix} 14 \cdot 1 \\ 14 \cdot 1 \end{pmatrix}$	$\begin{pmatrix} 18.4 \\ 18.4 \end{pmatrix}$
133		1.263	225.85	227.7	3.4 43.5	45.8	10.0	0.5
104)	0001	1 959	229.18		10.0	20 0	(24.5)	(16.4)
142 }	2021	1.253	229·18 J		20·0 J		$(24 \cdot 5)$	(16.4)
330		1.238	235.05		1.6		10.0	0.5
241			237.62		0		0	0
322		1.927	230.17	238.0	3.9	3.5	10.0	0.5
331		$1 \cdot 204$	248.36	248·5	$\frac{52}{2 \cdot 9}$	3.1	10.0	0.5
024			253.00		0		0	0
400	0004	1.181	258.08	257.6	13.2	12.6	42.3	$19 \cdot 2$
150		1.164	265·80		1.4		10.0	0.5
124			209.13 974.94		0		0	0
313		1.144	275.00		2.8		10.0	0.5
204)	2022		277.57	070.1	11.0		(28.3)	(9.8)
242	2022	1.139	277.57	276-1	22.0 $38.5$	37.5	28.3	9.8
151		1.135	279.11 J		2·7 J		`10-0΄	`0·5 <sup>′</sup>
043			279.63	—	0		0	0
411 914			281.38	—	0		0	0
214 332		1.117	287.90 288.31	288.7	U 9.6	2.1	0 10.0	0.5
143			295.76		0		0	0.5
420			298.03		Ō		Õ	Õ

changes at all and was assumed to be constant. The agreement between calculated and observed intensities is remarkable, although the measurement of the high angle lines due to broadening is somewhat difficult.

The X-ray and neutron diffraction patterns compared in Fig. 1 show some interesting features. The X-ray scattering factor for carbon in comparison to that for molybdenum is practically zero. Thus, as is well known, the X-ray diffraction pattern will reveal only the molybdenum partial structure, a hexagonal close-packed arrangement. Otherwise, in the case of neutron diffraction, carbon and molybdenum have exactly the same neutron scattering amplitude of  $b_{M_0} = b_C = 0.661 \times 10^{-12}$  cm. Thus the Mo<sub>2</sub>C structure will behave like a more complicated element structure to neutrons. This leads to the uncommon situation that some diffraction lines occur in the X-ray diffraction pattern that do not occur in the neutron diffraction pattern (002/021 and 004/042)and also vice versa (110, 111 etc.). This is illustrated in the last two columns of Table 1 which allow a comparison between the  $|{}^{\circ}F|$  values for neutron- and X-ray diffraction.

## Discussion of the Mo<sub>2</sub>C structure

Mo<sub>2</sub>C is a member of the family of interstitial or Hägg compounds as they occur with TiC, WC or MoC. Fig. 2



Fig. 2. Atom positions in Mo<sub>2</sub>C.

shows the nets of the hexagonal closed-packed molybdenum atoms with the carbon atoms placed in octahedral voids. While in the  $CdI_2$  structure proposal the carbon atoms would be in one layer only, or according to L'3 distributed randomly about all possible sites, the carbon atoms in Mo<sub>2</sub>C arrange themselves in both layers (0 and 1/2) in a systematic way. This particular arrangement lets every molybdenum atom have three equidistant carbon atom neighbours, whereby the three carbon atoms and the molybdenum atom are very nearly in one plane. The construction formula (Laves, 1956; Parthé, 1961) of Mo<sub>2</sub>C can be calculated to be

Mo 3	sl -	6 C
<u> </u>		↓
12L		2C
1.40(6)		1.43
1.43(6)		

Four carbides:  $V_2C$ ,  $Nb_2C$ ,  $Ta_2C$  and  $W_2C$ —and also a few nitrides like  $Ta_2N$  are known from X-ray data to be isostructural with Mo<sub>2</sub>C. But a recent electron diffraction study on  $W_2C$  by Butorina & Pinsker (1960) has shown that  $W_2C$  has the anti-cadmium iodide structure type. It might be worthwhile to investigate  $W_2C$  and all other sesquicarbides and nitrides by neutron diffraction technique.

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